



Hands-on Introduction to Deep Learning

Convolutional Neural Networks



INSTITUT DU
DÉVELOPPEMENT ET DES
RESSOURCES EN
INFORMATIQUE
SCIENTIFIQUE

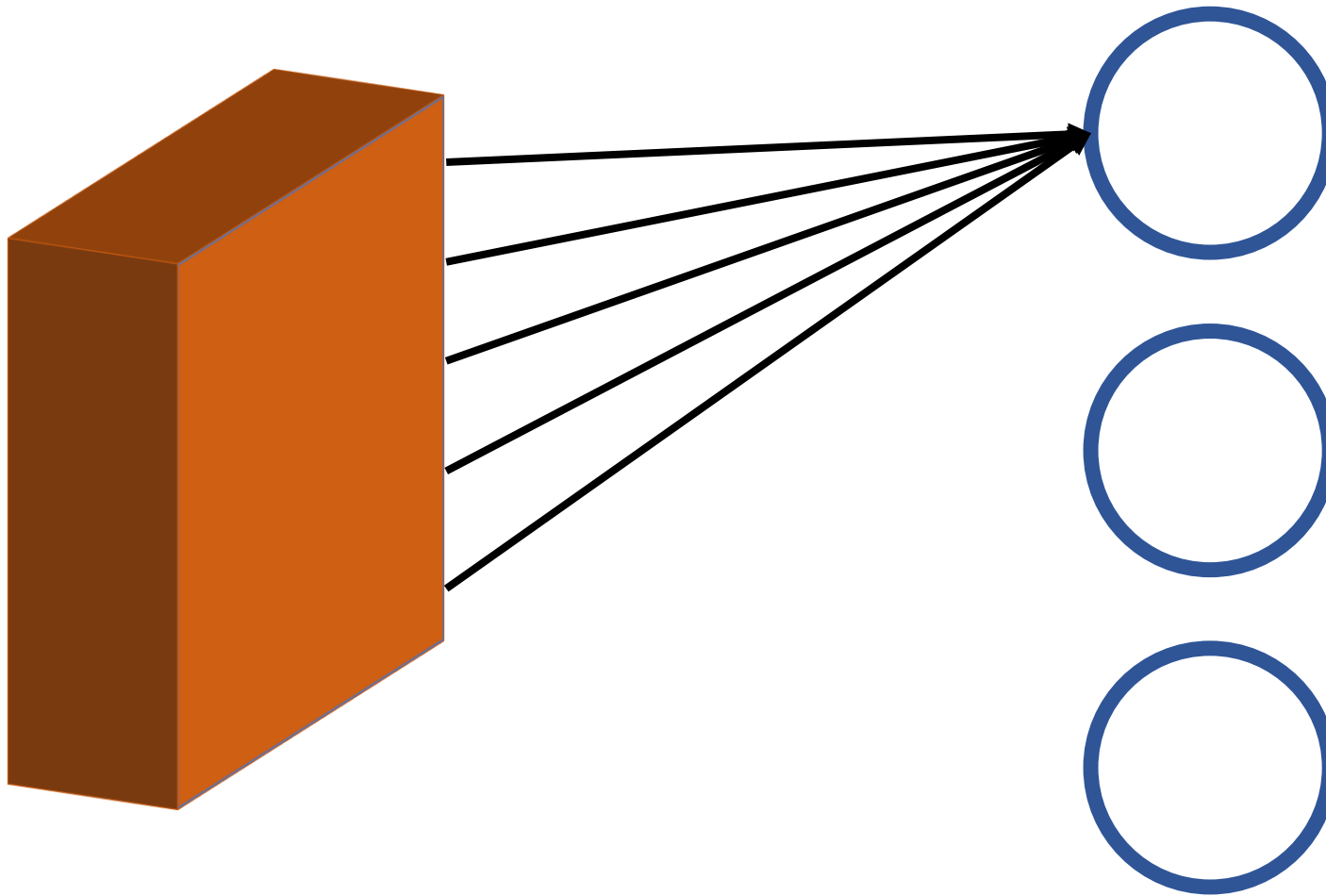


Image : 3 x 5 x 5

**1 layer, 3 neurons :
75 weights per neuron**

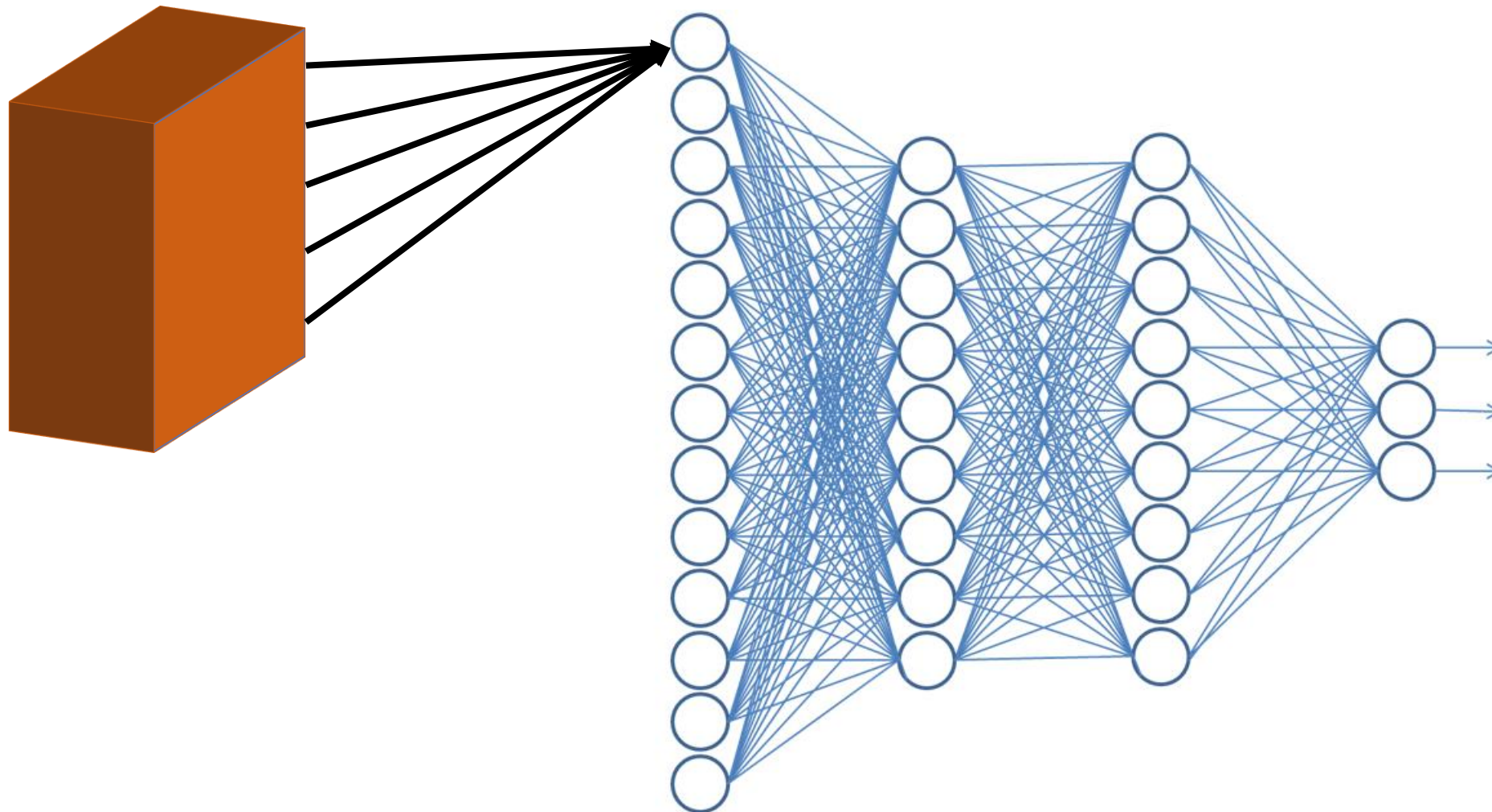


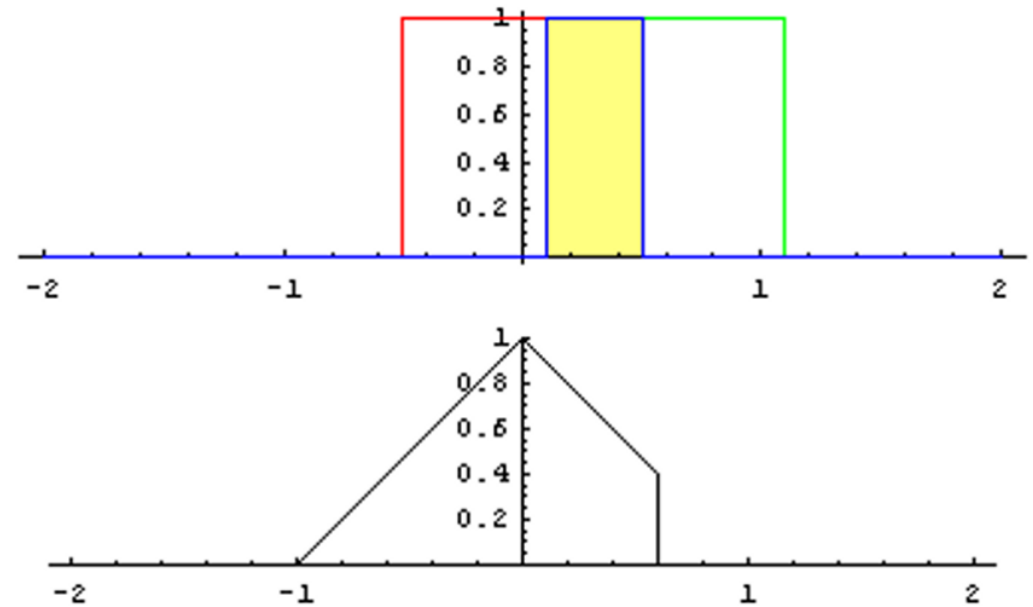
Image : 3 x Height x Width

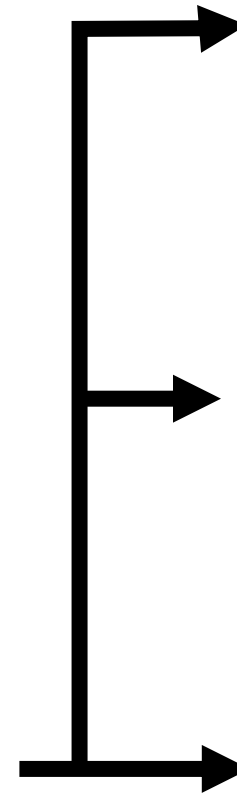
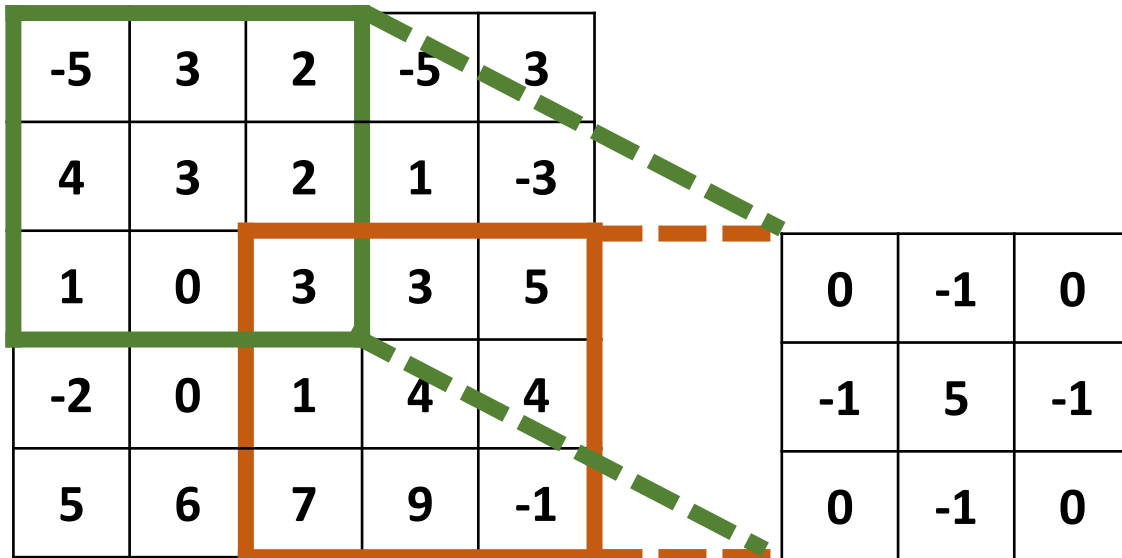
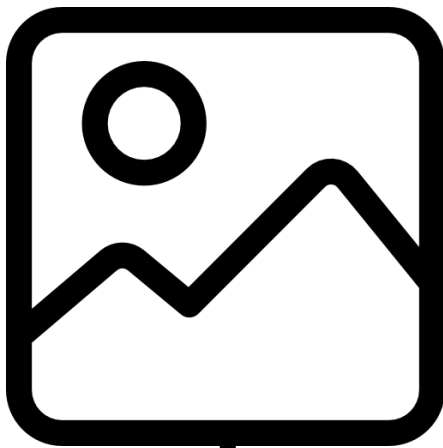
Complex model

$$f * g = \int_{-\infty}^{\infty} f(\tau)g(t - \tau)d\tau$$



$$f * g = \sum_{\substack{0 \leq i \leq n \\ 0 \leq j \leq m}} f(x_{i,j})g(x_{k-i,l-j})$$





6		



6	1	8
-7	9	2
-5	-9	3



Edge detection

$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$



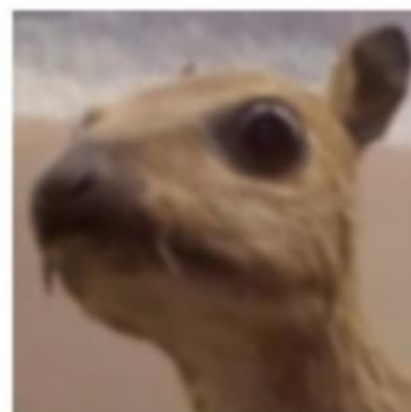
Box mean

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$



Sharpen

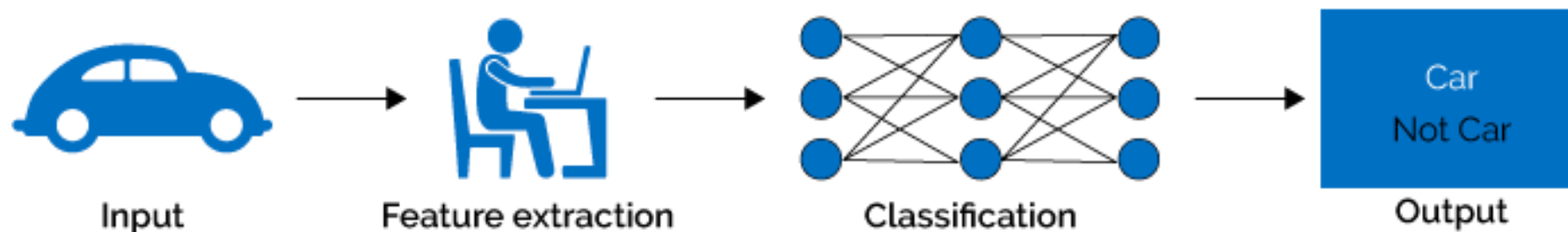
$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$



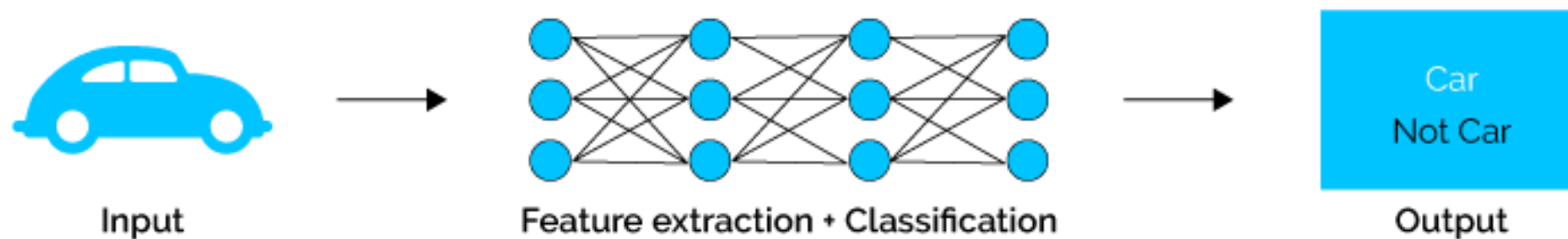
Gaussian blur

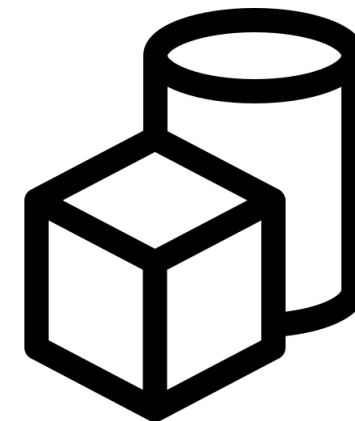
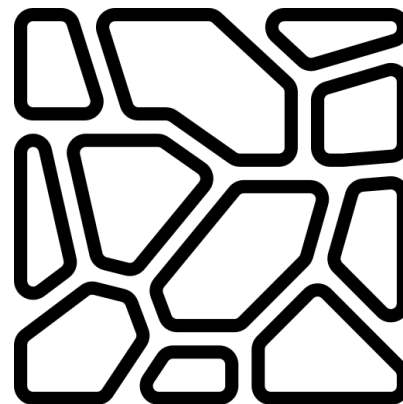
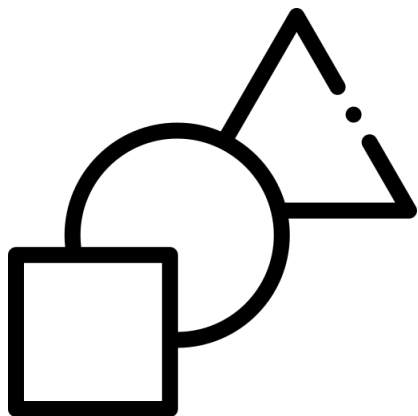
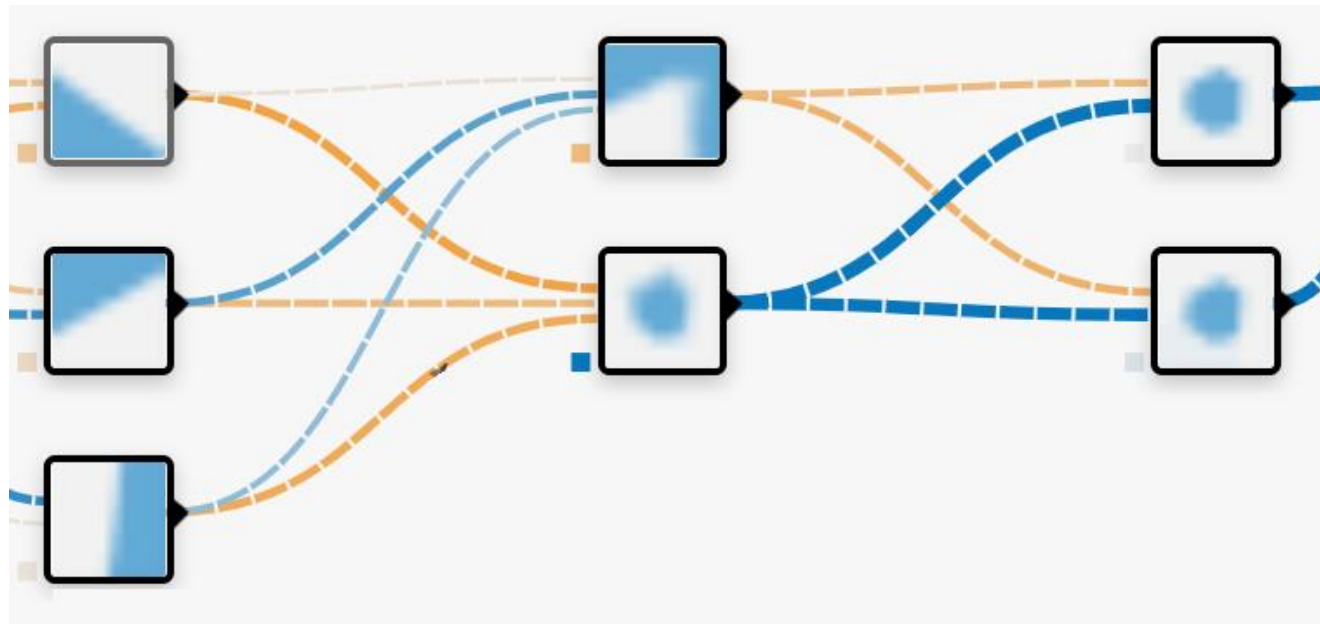
$$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

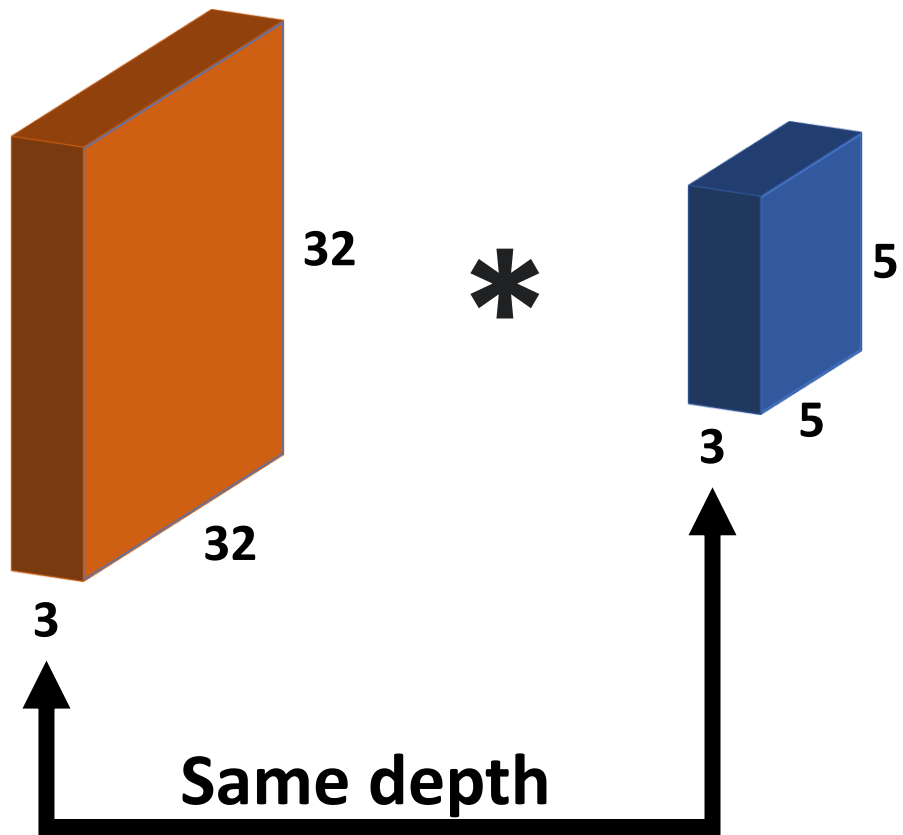
Machine Learning



Deep Learning

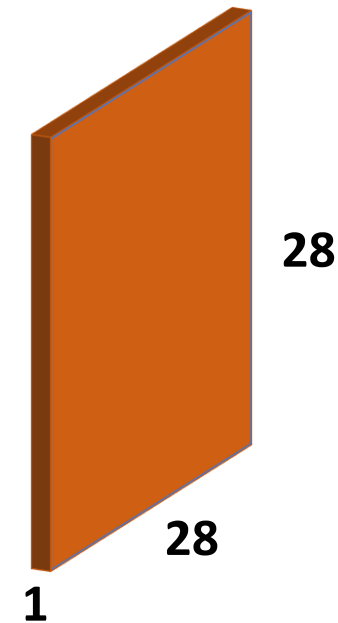


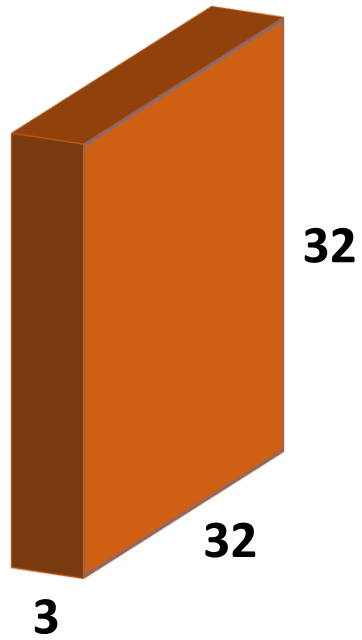




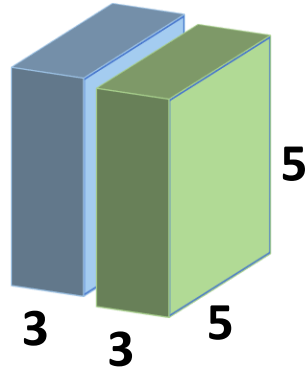
Convolution

Activation | Feature Map

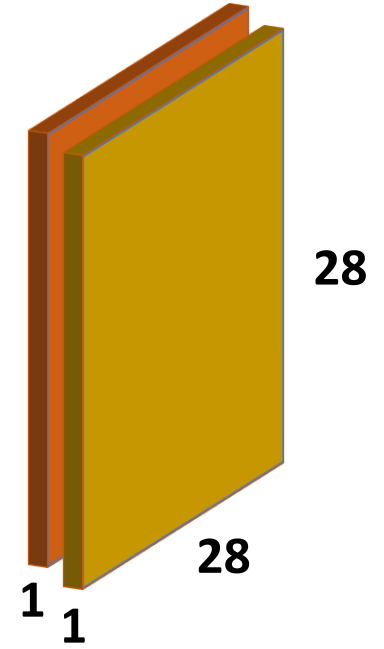


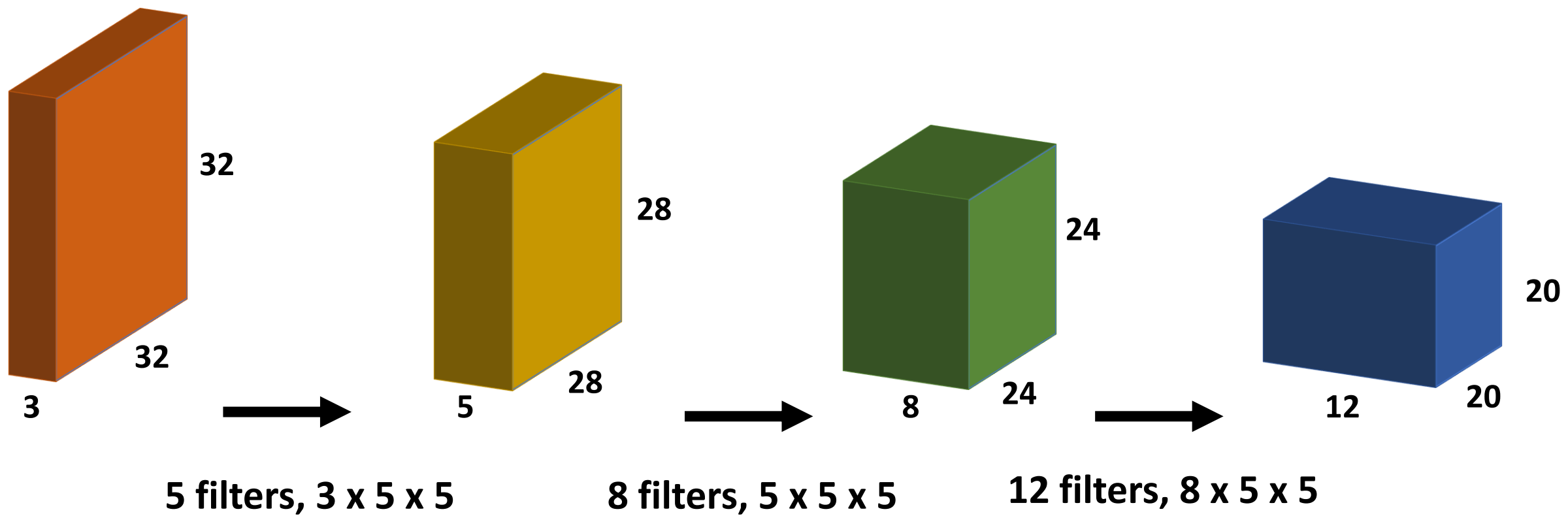


*



Convolution



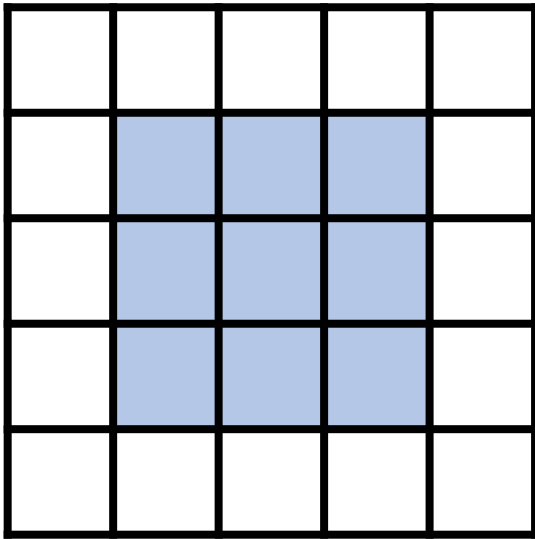


0	0	0	0	0	0	0
0	-5	3	2	-5	3	0
0	4	3	2	1	-3	0
0	1	0	3	3	5	0
0	-2	0	1	4	4	0
0	5	6	7	9	-1	0
0	0	0	0	0	0	0

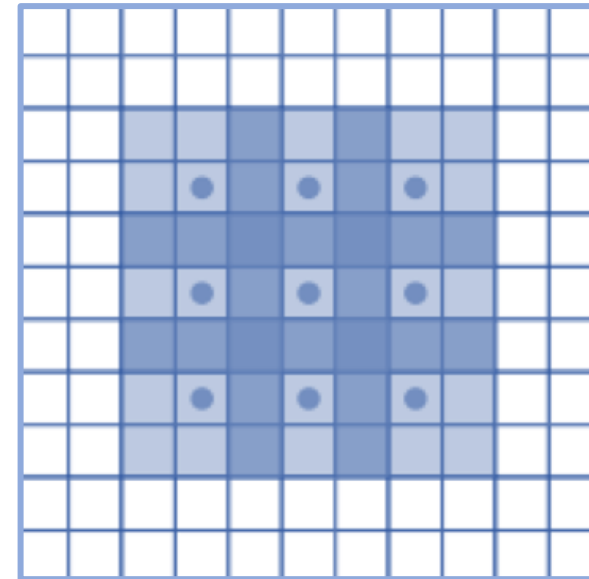
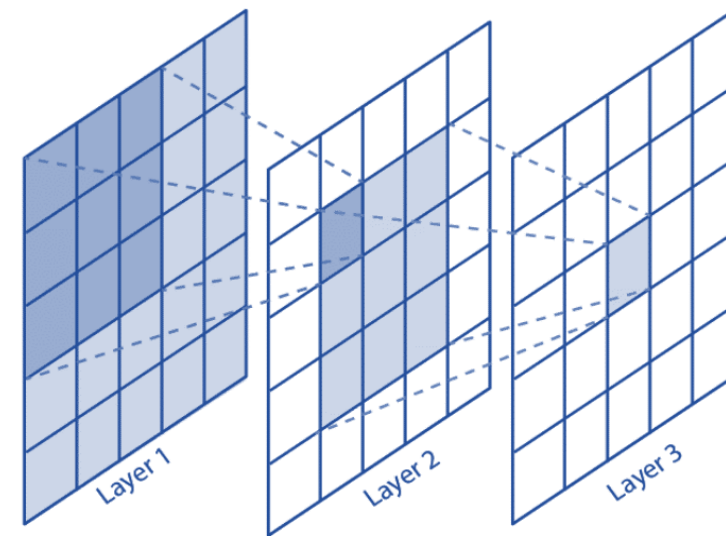
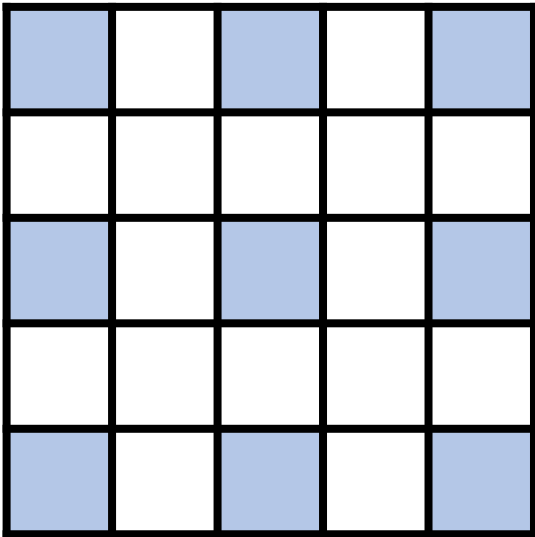
Output: $\left(\frac{N+2\cdot P-F}{S} + 1\right) \times \left(\frac{N+2\cdot P-F}{S} + 1\right)$

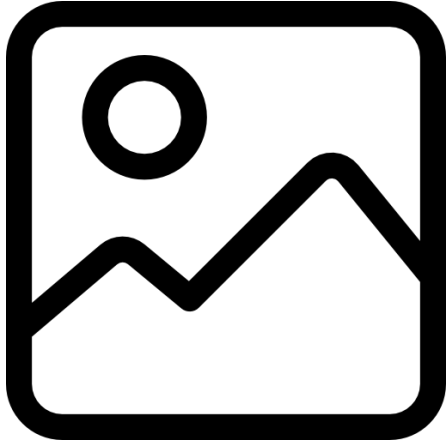
- **Entrée : 5 x 5**
- **Filtre : 3 x 3**
- **Padding : 1**
- **Stride : 1**
- **Sortie : 5 x 5**

D = 1

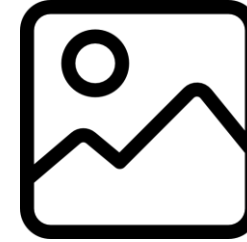


D = 2





Compression



5	3	1	9
2	4	5	6
7	8	5	6
1	3	4	5



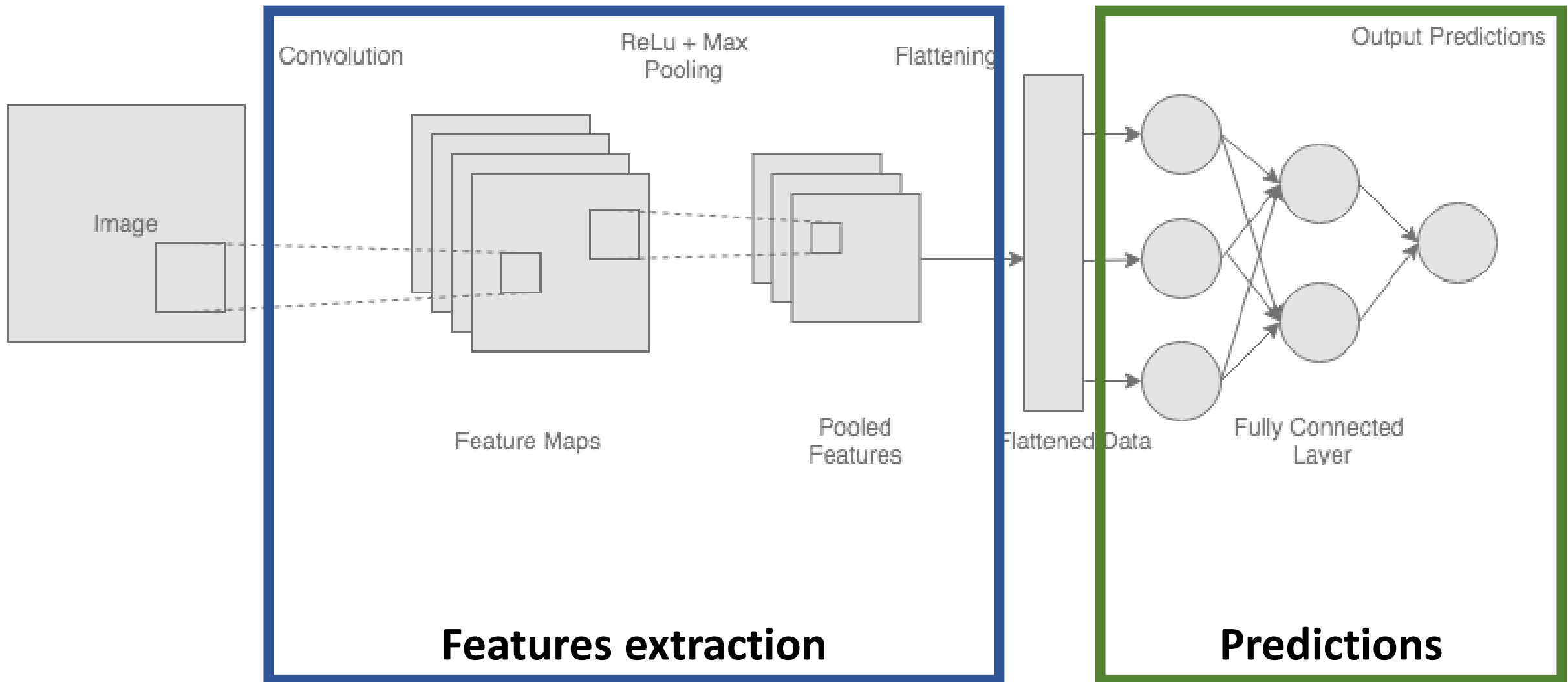
Max Pooling
Filter : 2 x 2
Stride : 2

5	9
8	6



Mean Pooling
Filter : 2 x 2
Stride : 2

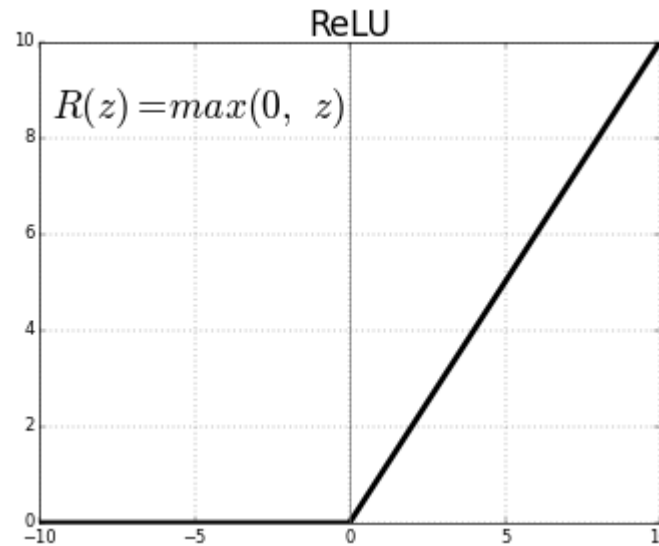
3,5	5,25
4,75	5



-5	3	2	-5	3
4	3	2	1	-3
1	0	3	3	5
-2	0	1	4	4
5	6	7	9	-1



0	3	2	0	3
4	3	2	1	0
1	0	3	3	5
0	0	1	4	4
5	6	7	9	0



```
import torch.nn as nn
import torch.nn.functional as F
```

```
class Net(nn.Module):
```

```
    def __init__(self):
```

```
        super().__init__()
```

```
        self.conv1 = nn.Conv2d(3, 6, 5)
```

```
        self.pool = nn.MaxPool2d(2, 2)
```

```
        self.conv2 = nn.Conv2d(6, 16, 5)
```

```
        self.fc1 = nn.Linear(16 * 5 * 5, 120)
```

```
        self.fc2 = nn.Linear(120, 84)
```

```
        self.fc3 = nn.Linear(84, 10)
```

```
    def forward(self, x):
```

```
        x = self.pool(F.relu(self.conv1(x)))
```

```
        x = self.pool(F.relu(self.conv2(x)))
```

```
        x = torch.flatten(x, 1) # flatten all dimensions except batch
```

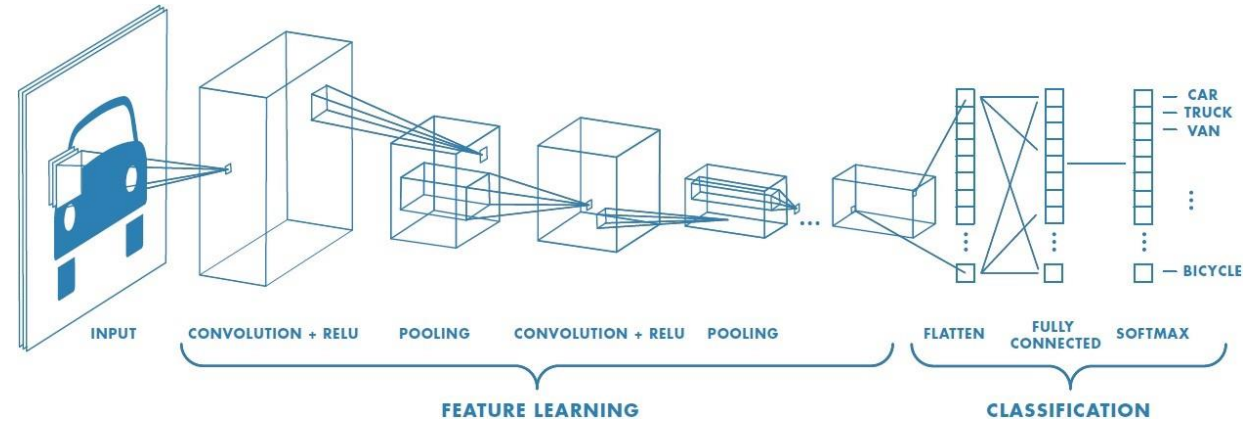
```
        x = F.relu(self.fc1(x))
```

```
        x = F.relu(self.fc2(x))
```

```
        x = self.fc3(x)
```

```
        return x
```

```
net = Net()
```



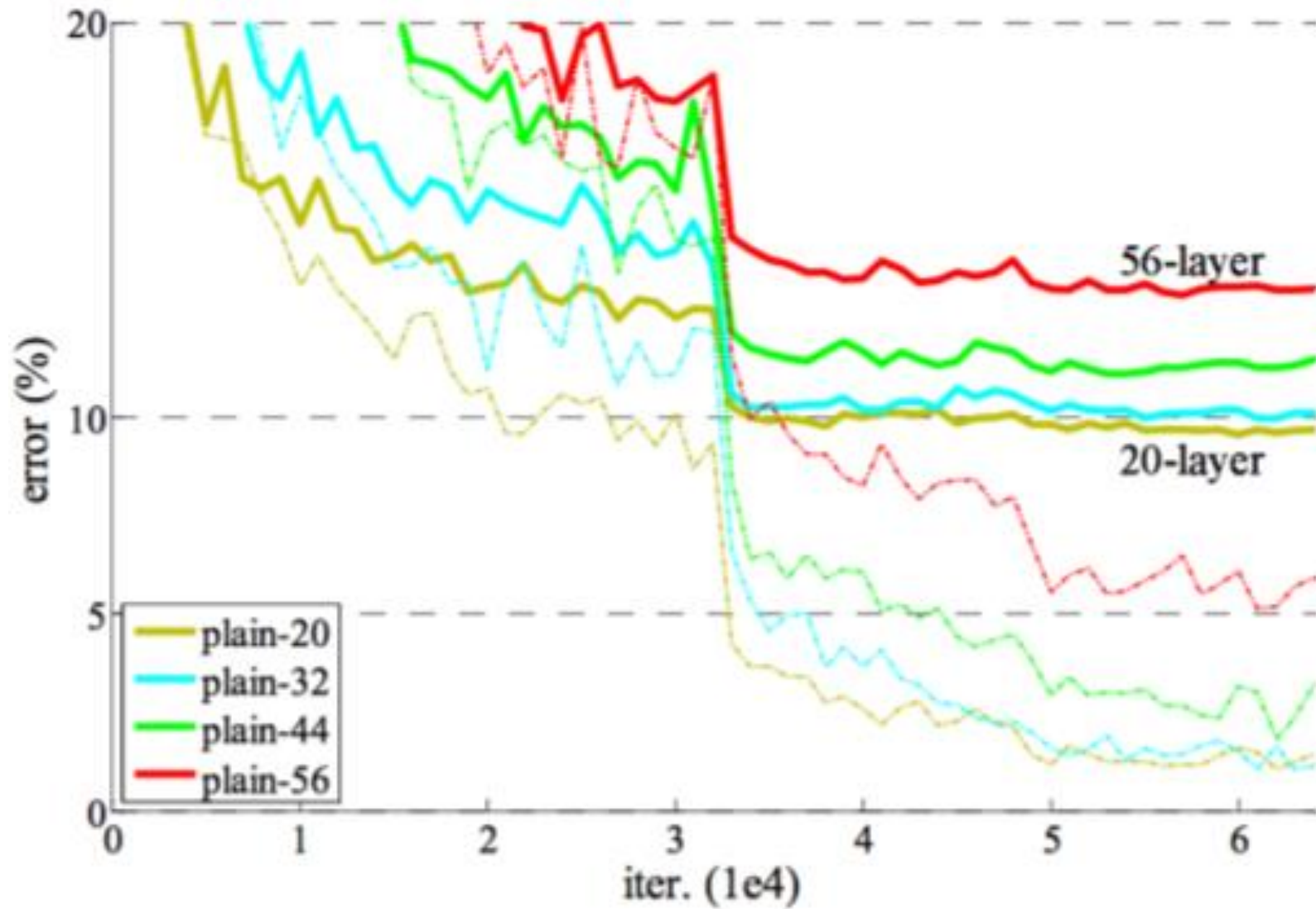
```
torch.nn.Conv2d(
    in_channels,
    out_channels,
    kernel_size,
    stride=1,
    padding=0,
    dilation=1,
    groups=1,
    bias=True,
    padding_mode='zeros',
    device=None,
    dtype=None)
```

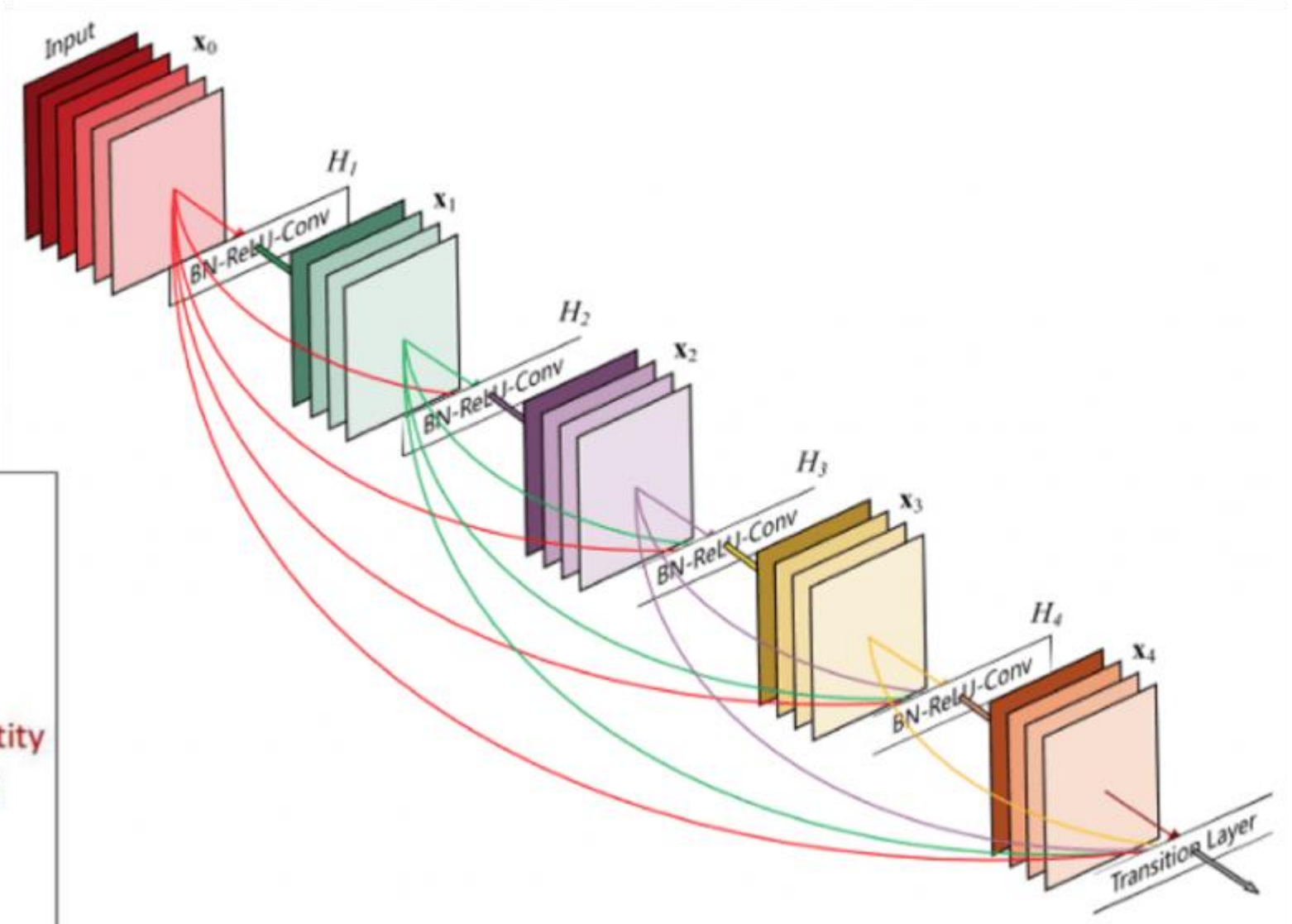
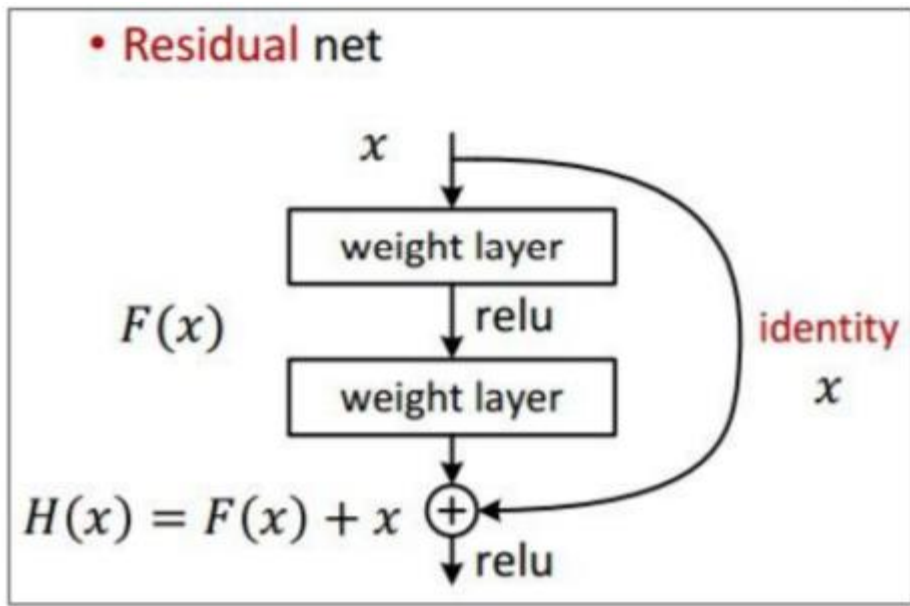
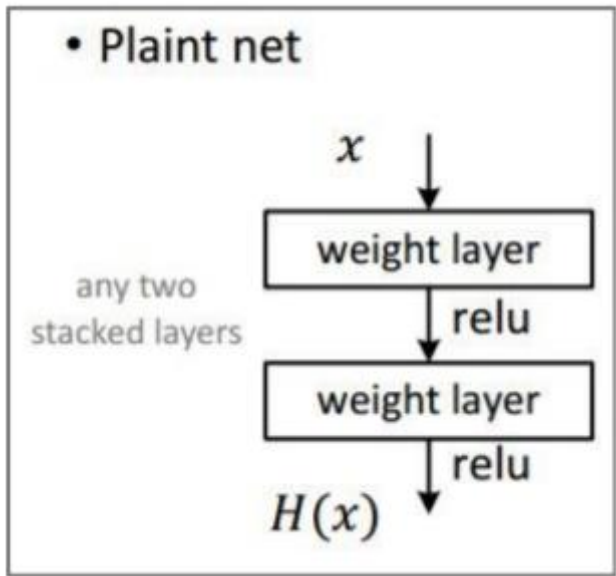
$$\begin{array}{|c|c|} \hline O_{11} & O_{12} \\ \hline O_{21} & O_{22} \\ \hline \end{array} = \text{Convolution} \left(\begin{array}{|c|c|c|} \hline X_{11} & X_{12} & X_{13} \\ \hline X_{21} & X_{22} & X_{23} \\ \hline X_{31} & X_{32} & X_{33} \\ \hline \end{array} , \begin{array}{|c|c|} \hline F_{11} & F_{12} \\ \hline F_{21} & F_{22} \\ \hline \end{array} \right)$$

Output O Input X Filter F

$$\begin{array}{|c|c|c|} \hline \frac{\partial L}{\partial X_{11}} & \frac{\partial L}{\partial X_{12}} & \frac{\partial L}{\partial X_{13}} \\ \hline \frac{\partial L}{\partial X_{21}} & \frac{\partial L}{\partial X_{22}} & \frac{\partial L}{\partial X_{23}} \\ \hline \frac{\partial L}{\partial X_{31}} & \frac{\partial L}{\partial X_{32}} & \frac{\partial L}{\partial X_{33}} \\ \hline \end{array} = \text{Full Convolution} \left(\begin{array}{|c|c|} \hline F_{22} & F_{21} \\ \hline F_{12} & F_{11} \\ \hline \end{array} , \begin{array}{|c|c|} \hline \frac{\partial L}{\partial O_{11}} & \frac{\partial L}{\partial O_{12}} \\ \hline \frac{\partial L}{\partial O_{21}} & \frac{\partial L}{\partial O_{22}} \\ \hline \end{array} \right)$$

$\frac{\partial L}{\partial X}$ Filter F Loss Gradient $\frac{\partial L}{\partial O}$

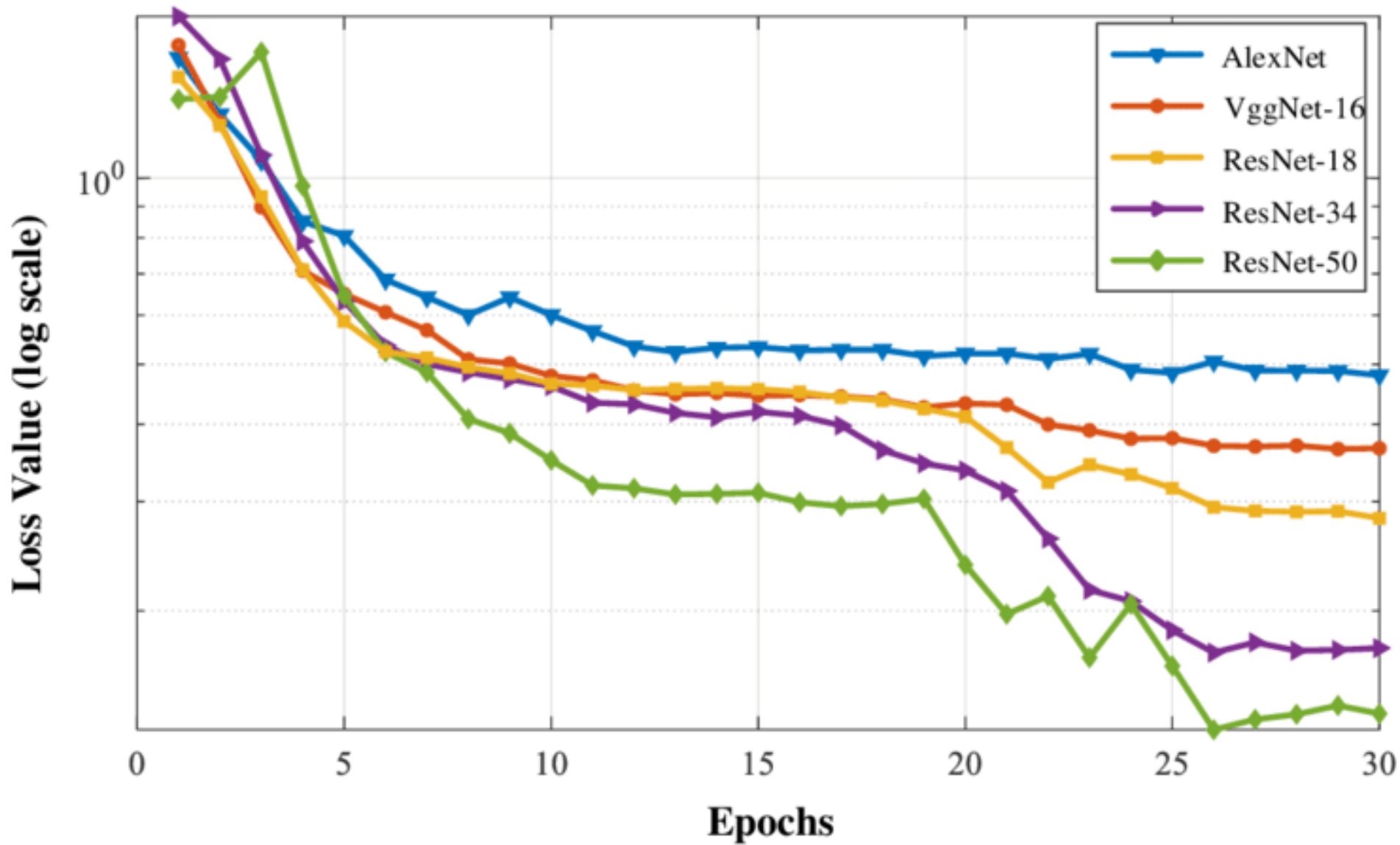




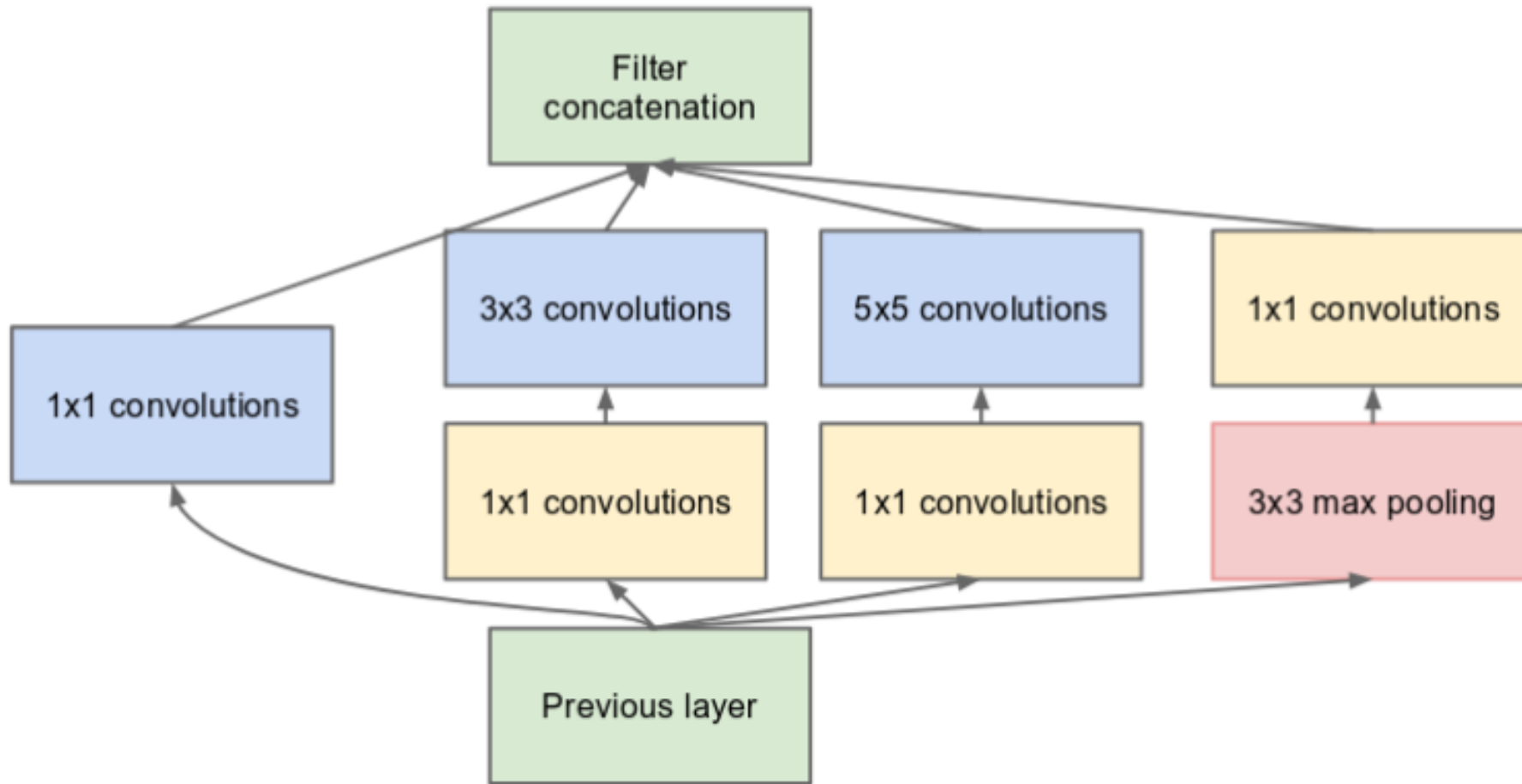
He, Kaiming, et al. "Deep residual learning for image recognition."

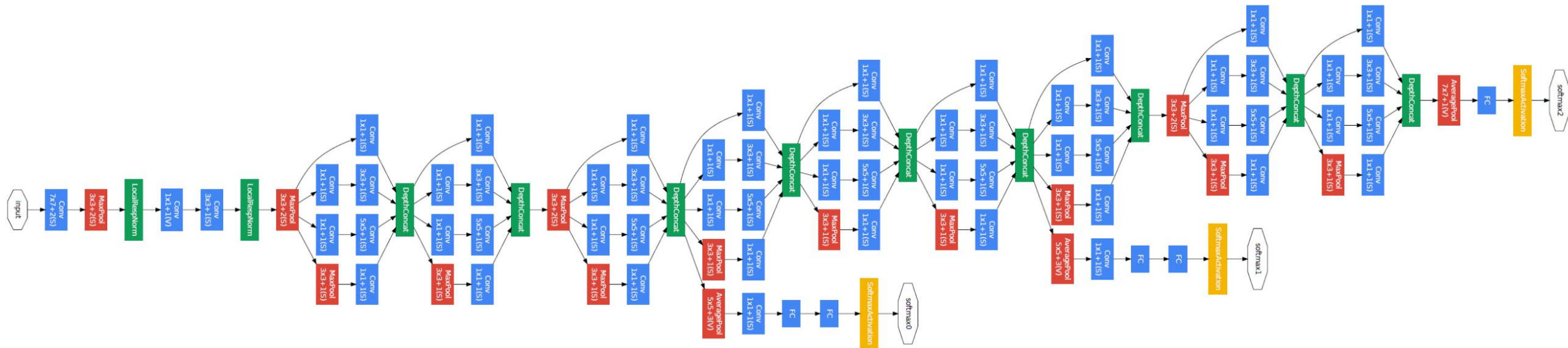


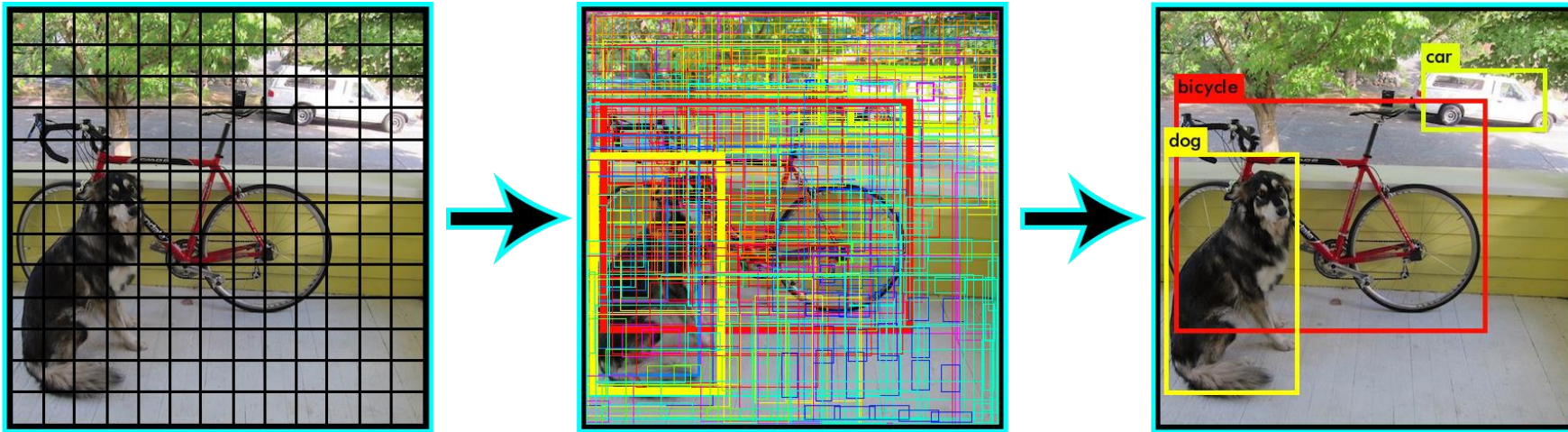
ResNet



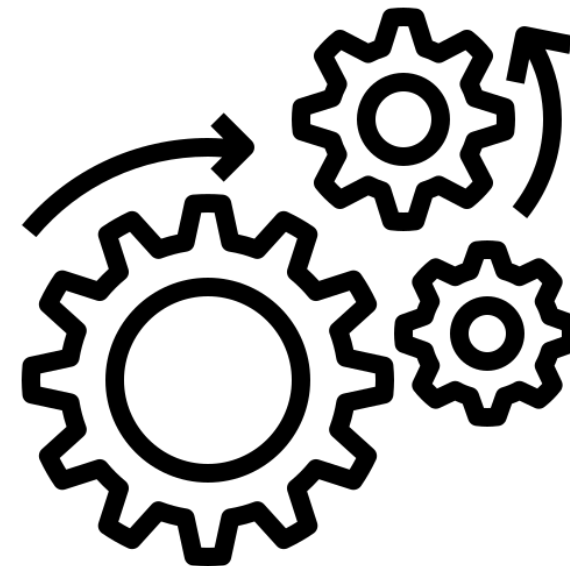
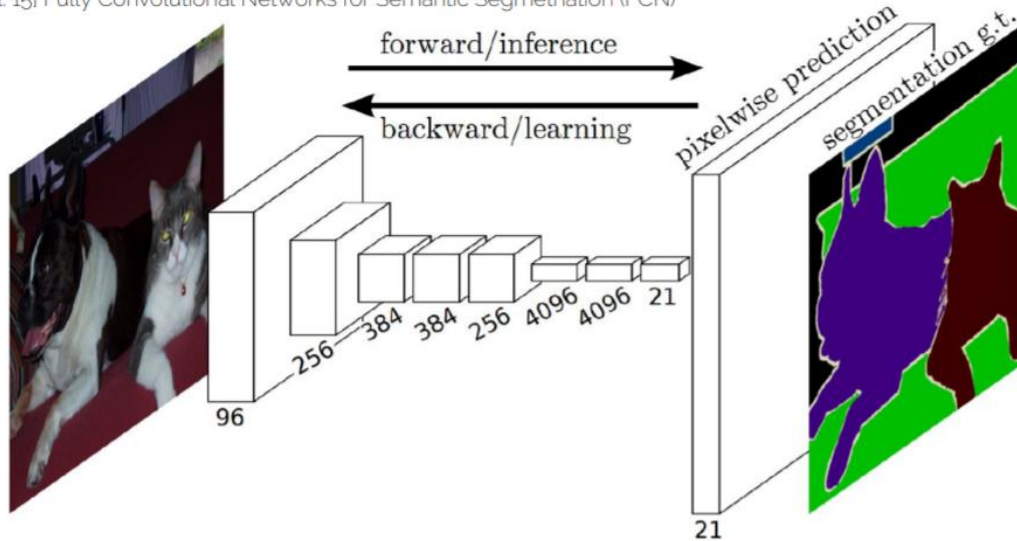
He, Kaiming, et al. "Deep residual learning for image recognition."







[Long et al. 15] Fully Convolutional Networks for Semantic Segmentation (FCN)



Redmon, Joseph, et al. "You only look once: Unified, real-time object detection."
 Long, et al "Fully convolutional networks for semantic segmentation."